

16.1 An alternating current is represented by the equation $I = 20 \sin 100\pi t$. Compute its frequency and the maximum and rms values of current.

Solution . The standard equation for A.C is

$$I = I_0 \sin(2\pi ft) \quad \text{--- (1)}$$

The given equation is

$$I = 20 \sin(100\pi t) \quad \text{--- (2)}$$

(a) Frequency

Comparing eq (1) and (2)

$$2\pi f = 100\pi$$

$$f = \frac{100\pi}{2\pi}$$

$$f = 50 \text{ Hz}$$

(b) Maximum Current

Again by comparing (1) and (2)

$$I_0 = 20 \text{ A}$$

(c) rms value of current

$$\text{As } I_{\text{rms}} = \frac{I_0}{\sqrt{2}} = 0.707 I_0$$

$$I_{\text{rms}} = 0.707 \times 20 \text{ A}$$

$$I_{\text{rms}} = 14 \text{ A}$$

16.2 A sinusoidal A.C. has a maximum value of 15 A. What are its rms values? If the time is recorded from the instant the current is zero and is becoming positive, what is the instantaneous value of the current after $\frac{1}{300}$ s given the frequency is 50 Hz?

Solution $I_0 = 15 \text{ A}$, $t = \frac{1}{300} \text{ s}$, $f = 50 \text{ Hz}$
rms - value. $I_{\text{rms}} = ?$, $I = ?$

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}} = 0.707 I_0$$

$$I_{\text{rms}} = 0.707 \times 15 \text{ A}$$

$$I_{\text{rms}} = 10.6 \text{ A}$$

Instantaneous Value of Current

$$I = I_0 \sin \omega t = I_0 \sin 2\pi f t$$

$$I = 15A \sin(2\pi \times 50 \times \frac{1}{300})$$

$$I = 15A \sin(\frac{\pi}{3}) = 15A \sin(180/3) = 15A \sin 60^\circ$$

$$I = 15A \times 0.866 = 12.96A$$

$$I = 13.0A$$

16.3 :- Find the value of the current and inductive reactance when A.C. voltage of 220V at 50 Hz is passed through an inductor of 10H.

Solution :- $V = 220V$, $f = 50 \text{ Hz}$, $L = 10H$
 $I = ?$ $X_L = ?$

Inductive Reactance.

$$X_L = \omega L = 2\pi f L$$

$$X_L = 2 \times 3.14 \times 50 \text{ Hz} \times 10H$$

$$X_L = 3140 \Omega$$

Current -

$$I = \frac{V}{X_L} = \frac{220V}{3140 \Omega}$$

$$I = 0.07A$$

16.4 :- A circuit has an inductance of $\frac{1}{\pi} H$ and resistance of 2000Ω . A 50 Hz A.C. is supplied to it. Calculate the reactance and impedance offered by the circuit.

Solution :- $L = \frac{1}{\pi} H$, $R = 2000 \Omega$, $f = 50 \text{ Hz}$
 $X_L = ?$ $Z = ?$

Reactance

$$X_L = \omega L = 2\pi f L$$

$$X_L = 2 \times 3.14 \times 50 \text{ Hz} \times \frac{1}{3.14} H$$

$$X_L = 100 \Omega$$

Impedance

$$Z = \sqrt{R^2 + (X_L)^2} = \sqrt{(2000)^2 + (100)^2} \Omega$$

$$Z = 2002.5 \Omega$$

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$$\text{As } V = IZ$$

$$I = \frac{V}{Z} = \frac{240 \text{ V}}{20.3214 \Omega} = 11.81 \text{ A}$$

Now

$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right) = \tan^{-1}\left(\frac{3.6}{20}\right) = 10.20^\circ$$

$$\text{Power Dissipated} = P = VI \cos \phi$$

$$= 240 \text{ V} \times 11.81 \text{ A} \cos 10.20^\circ$$

$$P = 2389.6 \text{ W}$$

16.7 Find the value of the current flowing through a capacitance $0.5 \mu\text{F}$ when connected to a source of 150 V at 50 Hz .

Solution :- $C = 0.5 \times 10^{-6} \text{ F}$, $V = 150 \text{ V}$, $f = 50 \text{ Hz}$

$I = ?$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} = \frac{1}{2 \times 3.14 \times 50 \text{ s}^{-1} \times 0.5 \times 10^{-6} \text{ F}}$$

$$X_C = 6369.4 \Omega$$

then Current = $I = \frac{V}{X_C}$

$$I = 0.024 \text{ A}$$

16.8 An alternating source of emf 12 V and frequency 50 Hz is applied to a capacitor of capacitance $3 \mu\text{F}$ in series with a resistor of resistance 1Ω . Calculate the phase angle.

Solution :- $V = 12 \text{ V}$, $f = 50 \text{ Hz}$, $C = 3 \times 10^{-6} \text{ F}$, $R = 1 \Omega$

$\phi = ?$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} = \frac{1}{2 \times 3.14 \times 50 \text{ s}^{-1} \times 3 \times 10^{-6} \text{ F}} = \frac{10^6}{942}$$

$$X_C = 1062.89 \Omega$$

$$\phi = \tan^{-1}\left(\frac{X_C}{R}\right) = \tan^{-1}\left(\frac{1062.89 \Omega}{1 \Omega}\right)$$

$$\phi = 89.9^\circ$$

16.9 What is the resonating frequency of a circuit which includes a coil of inductance 2.5 H and a capacitance $40 \mu\text{F}$?

$L = 2.5 \text{ H}$, $C = 40 \times 10^{-6} \text{ F}$

$$f = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2 \times 3.14 \times \sqrt{2.5 \text{ H} \times 40 \times 10^{-6} \text{ F}}} = 15.9 \text{ Hz}$$

16.10 An inductor of inductance $150\mu\text{H}$ is connected in parallel with a variable capacitor whose capacitance can be changed from 500pF to 20pF . Calculate the maximum and minimum frequency for which the circuit can be tuned.

Solution

$$L = 150\mu\text{H} = 150 \times 10^{-6} \text{H}$$

$$C_1 = 500\text{pF} = 500 \times 10^{-12} \text{F}$$

$$C_2 = 20\text{pF} = 20 \times 10^{-12} \text{F}$$

As resonating frequency = $f = \frac{1}{2\pi\sqrt{LC}}$ $f \propto \frac{1}{\sqrt{C}}$

So $f_{\text{min.}} = \frac{1}{2\pi\sqrt{LC_1}} = \frac{1}{2 \times 3.14 \times \sqrt{150 \times 10^{-6} \text{H} \times 500 \times 10^{-12} \text{F}}}$

$$f_{\text{min.}} = 0.58 \times 10^6 \text{ Hz} = 0.58 \text{ MHz}$$

and

$$f_{\text{max.}} = \frac{1}{2\pi\sqrt{LC_2}} = \frac{1}{2 \times 3.14 \times \sqrt{150 \times 10^{-6} \text{H} \times 20 \times 10^{-12} \text{F}}}$$

$$f_{\text{max.}} = 2.91 \times 10^6 \text{ Hz} = 2.91 \text{ MHz}$$

Therefore

$$f_{\text{max.}} = 2.91 \text{ MHz}$$

and

$$f_{\text{min.}} = 0.58 \text{ MHz}$$